

Motivation & Overview of the MAGNET Framework

Motivation

- High-fidelity computational models can be too slow for practical use, leading to the need for faster surrogate models.
- Deep learning techniques are being increasingly used to accelerate simulations, but struggle with larger and complex problems.

Solution

- A novel geometric deep learning framework for mesh based simulations.
- New neural network layers for graph-structured data such as meshes.

Implementation

- Proposed networks are trained on synthetic non-linear FEM datasets.
- Validated against state-of-the-art CNN U-Net framework [2, 3].

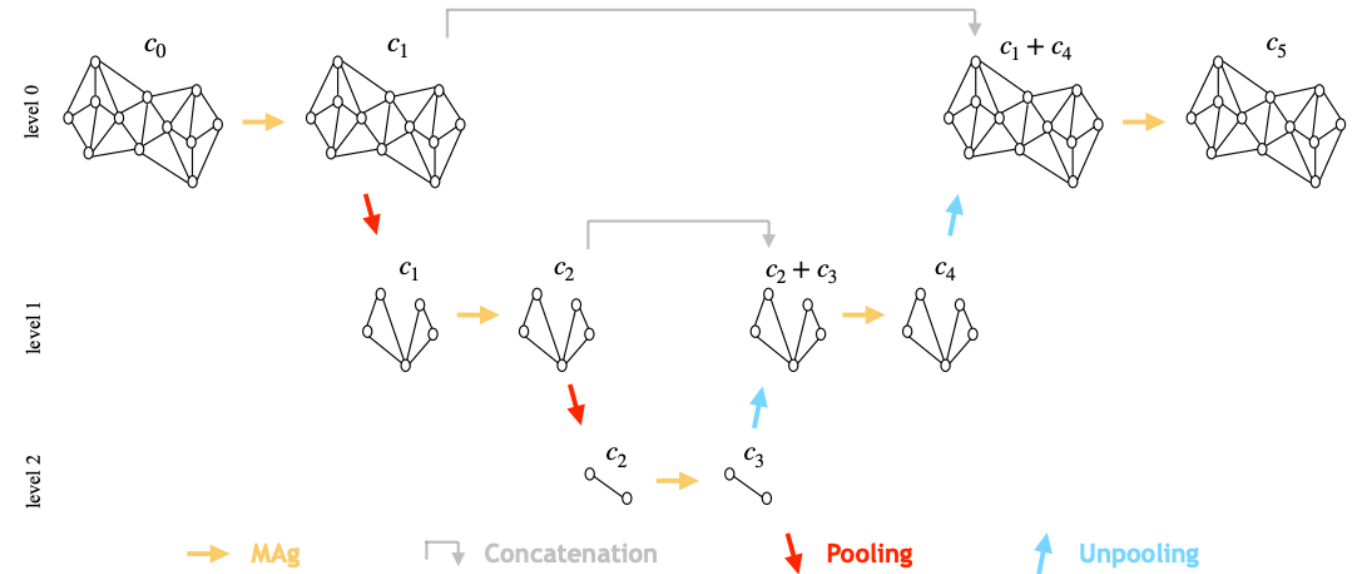


Figure 1. MAGNET: Multi-channel aggregation network [1].

Data Generation

Dataset $\mathcal{D} = (\mathbf{f}_i, \mathbf{u}_i)_{i=1}^N$, of pairs of nodal force, and displacement vectors is generated by applying random forces, using Neo-hookean hyperelastic law.

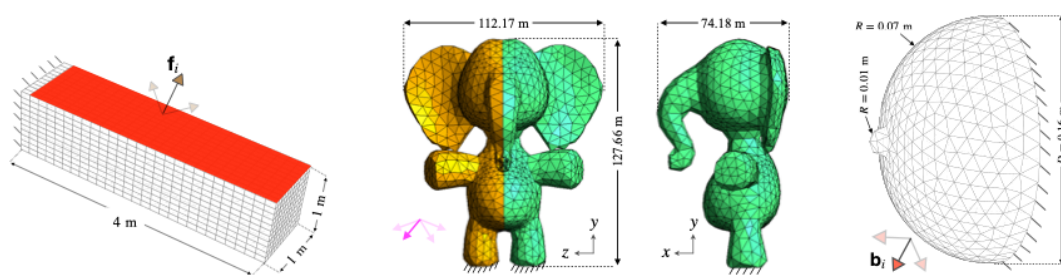


Figure 2. Schematics of three benchmark examples. Regions marked in red color indicate the nodes at which random nodal forces are applied to generate training datasets.

Training & Test Metrics

Training Loss: $\mathcal{L}_{\text{train}} = \frac{1}{N} \sum_{i=1}^N \|\mathcal{G}(\mathbf{f}_i) - \mathbf{u}_i\|_2^2$

Validation metric

For the test set $\{(\mathbf{f}_1, \mathbf{u}_1), \dots, (\mathbf{f}_M, \mathbf{u}_M)\}$, \mathcal{F} =Degrees of freedom of mesh

$$e_m = \frac{1}{\mathcal{F}} \sum_{i=1}^{\mathcal{F}} |\mathcal{G}(\mathbf{f}_m)^i - \mathbf{u}_m^i|.$$

$$\bar{e} = \frac{1}{M} \sum_{m=1}^M e_m, \quad \sigma(e) = \sqrt{\frac{1}{M-1} \sum_{m=1}^M (e_m - \bar{e})^2}$$

Results

Accuracy:

Example	\mathcal{F}	N	M	\bar{e} [m]	$\sigma(e)$ [m]	Max disp [m]
Beam (MAGNET)	12096	33858	1782	0.8 E-3	0.7 E-3	1.47
Beam (CNN U-Net)				0.7 E-3	0.5 E-3	
Elephant (MAGNET)	5835	7600	400	8.9 E-3	1.9 E-3	140.01
3D breast (MAGNET)	3105			8.9 E-5	3.1 E-5	0.07

Table 1. Error metrics for the test sets.

Prediction times:

MAGNET offered **x40 speedup** in comparison to FEM simulations.

Reference

- S. Deshpande, S.P.A. Bordas, and J. Lengiewicz. *MAGNET: A Graph U-Net Architecture for Mesh-Based Simulations*. Arxiv 2023. DOI: <https://doi.org/10.48550/arXiv.2211.00713>.
- S. Deshpande, J. Lengiewicz, and S.P.A. Bordas. *Probabilistic Deep Learning for Real-Time Large Deformation Simulations*. Computer Methods in Applied Mechanics and Engineering, 2022. DOI: <https://doi.org/10.1016/j.cma.2022.115307>.
- S. Deshpande et al. *Convolution, aggregation and attention based deep neural networks for accelerating simulations in mechanics*. Frontiers in Materials, 2023. DOI: 10.3389/fmats.2023.1128954.

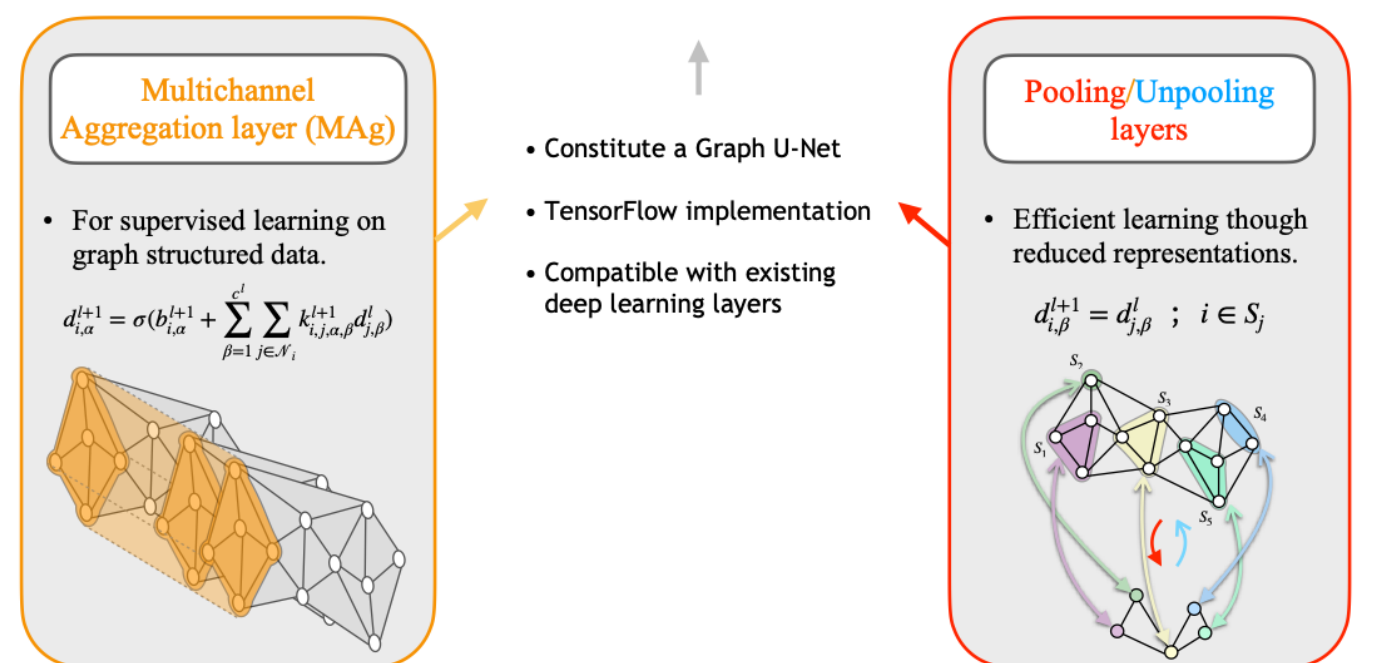
Acknowledgement

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Proposed Deep Learning Layers



Visualisations

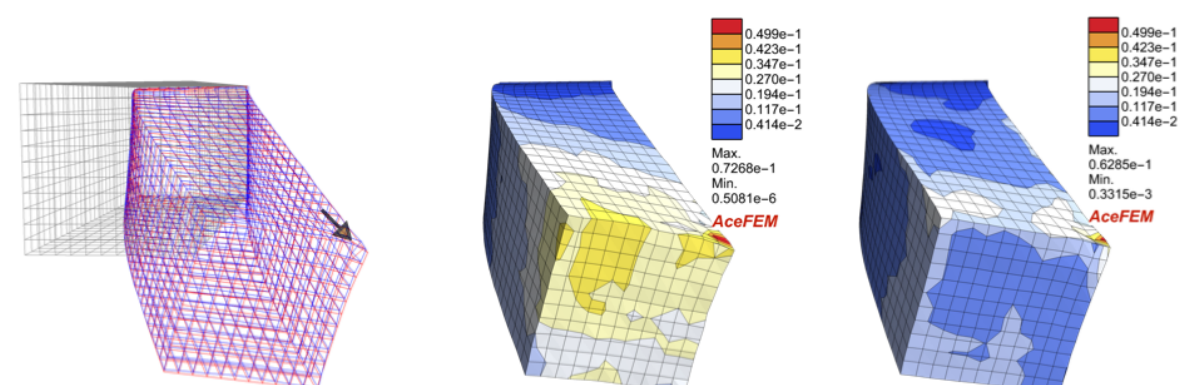


Figure 3. Deformation under point load. Error contours for MAGNET and CNN U-Net predictions, when compared to the FEM solution. The relative error for the prediction of displacement of node of application of load when compared to FEM is 4% for MAGNET and 3% for CNN U-Net.

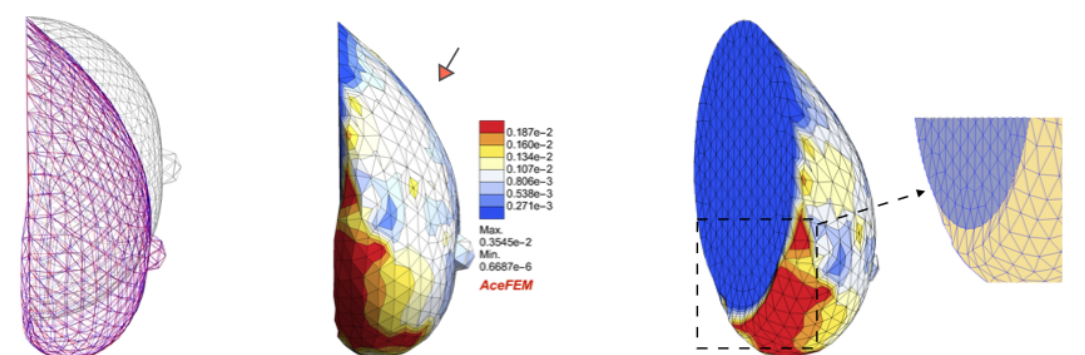


Figure 4. Deformation under body force computed using MAGNET. Maximum nodal displacement for this case is 0.07 m for the tip and relative prediction error for the same is 1%.

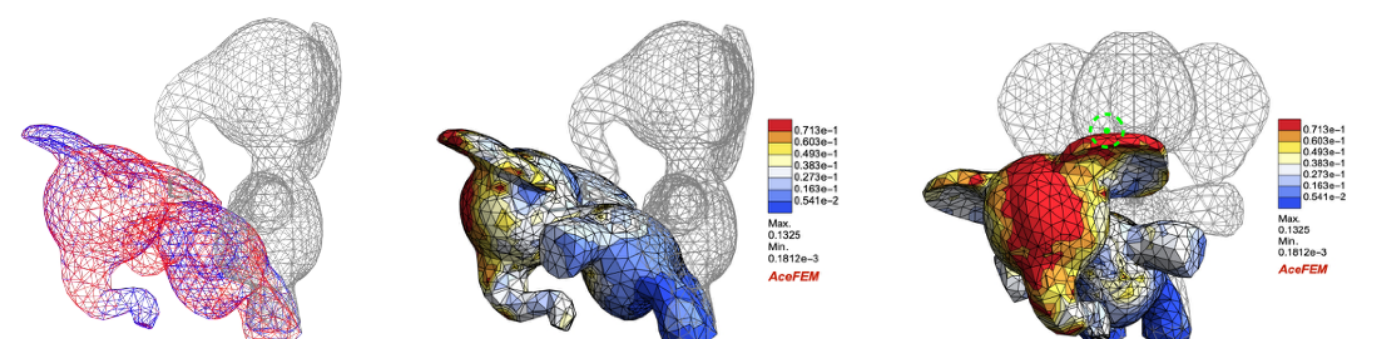


Figure 5. Deformation under body force computed using MAGNET. Maximum nodal displacement for this case is 140.01 m for the green node and relative prediction error for the same is 0.03%.

Conclusions

- MAGNET scales well and learns efficiently on arbitrary mesh inputs.
- MAG layer extended the concept of CNNs to non-grid inputs.
- MAGNET is an efficient surrogate model for non-linear FE simulations.